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## Leveraging Diversity



## Outline

Background: Two Inescapable Trends
Identity and Cognitive Diversity
Prediction
Case: Netflix Prize
Problem Solving
Takeaways

## Trend 1 Increasing Diversity

Race-Ethnic Profiles by Age Group, 2010

| $\square_{\text {White }}$ | $\square_{\text {Hispanic }}$ | $\square_{\text {Brack }} \square_{\text {atainn }}$ | $\square{ }_{\text {other }}$ | $\square_{\text {2+races }}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Unders year | $51 \%$ |  |  | [448 | \% |
| years | 55\% |  | 8 | 1468 | $4^{48)}$ |
| 18.35 years | 58\% |  |  | [13\% | 5\% \|l |
| 35.49 year | 64\% |  | $\pm$ | [2\% | 5\% \|1 |
| 50.64 years | [73\% |  |  | 118 | 4\%\|I |
| 65.74 years | [9\% |  |  | 9\% |  |
| ${ }^{85}$ y yars | 85\% |  |  |  | ${ }^{29}$ |

Source:Authar's anaysis of 2010 census dato

Countries/Regions Where Multinationals are Growing


## Black First-Year Enrollments

 in U.S. Medical Schools

Source: Association of American Medical Colleges.
Overall racial distribution in anthropology doctorate production, 1995-2007



Chicago


New York



## Normative Argument

Equalizing Opportunity.
Addressing past disadvantages.

## Pragmatic Advantages

Promoting diversity enlarges the pool.

Diversity
Ability

## Trend 2 Changing Nature of Work

## Employment by Industry - Percent of Total Workforce







## First 15 Nobels in Physics: 19 Winners

1901 Wilhelm C. Röntgen
1902 Hendrik A. Lorentz, Pieter Zeeman
1903 Antoine Henri Becquerel, Pierre Curie, Marie Curie
1904 John W. Strutt
1905 Philipp E. A. von Lenard
1906 Sir Joseph J. Thomson
1907 Albert A. Michelson
1908 Gabriel Lippmann
1909
1910
Carl F. Braun, Guglielmo Marconi
Johannes D. van der Waals
1911 Wilhelm Wien
1912 Nils G. Dalen
1913 Heike Kamerlingh Onnes
1914 Max von Laue
1915 William Bragg
$42$


Supercreative Employment: 331 U.S. MSAs 2003


## Diverse +

Group

## Rethinking



Want to understand how diversity affects group performance

## Diversity Ability



$$
\mathrm{E}[\mathrm{SqE}(\mathbf{c})]=B^{2}+\frac{1}{n} \operatorname{Var}+\frac{n-1}{n} \operatorname{Cov}
$$

two heads are better than one



## Identity and Cognitive Diversity



Zimbabwe


## Sweden




WESTERNERS AND EAST ASIANS DESCRIBE THIS SCENE IN DIFFERENT WAYS
(SOURCE: TME UNIVERSITY OF MICHICAN INSTITUTE FOR SOCIAL RESEARCN)


## The Ketchup Question




## Soda, Pop, or Coke By Region



Cultural Blinders
Poison RELS se pa manje rat vaszon Ral



Prediction


X lb?
Stars and Planets (astrology) Lightning
Rolling Dice Smoke and Fire
Flight of Birds Tarot Cards
Palm Reading MethodSeiofig of Horses
Atmospheric ConditionsNumbersDreams
Guessing
Animal Entrails

## Diverse Categorizations

## Linnean Classification Sort




Source: www.promotega.org

## Pile Sort



## BOBO Sort



## Airstream Sort



## Diversity Prediction Theorem

Crowd Error = Average Error - Diversity

$$
(c-\theta)^{2}=\frac{1}{n} \sum_{i=1}^{n}\left(s_{i}-\theta\right)^{2}-\frac{1}{n} \sum_{i=1}^{n}\left(s_{i}-c\right)^{2}
$$

## The Spherical Cow



## The Gateway Cow



## Galton' s Steer

Crowd Error = Average Error - Diversity

$$
0.6=2,956.0-2955.4
$$



## Case: Netflix Prize

## Outline

Netflix Prize: Background
Predictive Models
Factor Models
Ensembles of Models
Ensembles of Teams
The Value of Diversity

## Netflix Prize

November 2006, Netilix offers a prize of $\$ 1$ million to anyone who can defeat their Cinematch recommender system by $10 \%$ or more.

## Some Details

Netflix users rank movies from 1 to 5

Six years of data
Half million users
17,700 movies

Data divided into (training, testing)
Testing Data dived into (probe, quiz, test)

## Interesting Asides

Lost in Translation and The Royal Tenenbaums had the highest variance

Shawshank Redemption had the highest rating

Miss Congeniality had the most ratings.

## Singular Value Decomposition

Each movie represented by a vector:

$$
\left(p_{1}, p_{2}, p_{3}, p_{4} \ldots p_{n}\right)
$$

Each person represented by a vector:

$$
\left(q_{1}, q_{2}, q_{3}, q_{4}, \ldots q_{n}\right)
$$

Rating: $r_{j}=m_{i}+a_{j}+p \bullet q$
Training: choose $\mathrm{p}, \mathrm{q}$ to minimize

$$
\left(\text { actual }_{i j}-r_{\mathrm{ij}}\right)^{2}+c\left(\|p\|^{2}+\|q\|^{2}\right)
$$

## BellKor's Initial Models

Approximately 50 dimensions, 107 Models

Best Model: 6.8\% improvement

Combination of Models: 8.4\% improvement

## Why Do More Work Better?

$$
\begin{gathered}
\operatorname{SqE}(\mathrm{c})=\operatorname{SqE}(\mathrm{s})-\operatorname{PDiv}(\mathrm{s}) \\
(c-\theta)^{2}=\frac{1}{n} \sum_{i=1}^{n}\left(s_{i}-\theta\right)^{2}-\frac{1}{n} \sum_{i=1}^{n}\left(s_{i}-c\right)^{2}
\end{gathered}
$$

## BellKor's Pragmatic Chaos

More is Better: Seven person team

Functional Diversity: statisticians, machine learning experts and computer scientists

Identity Diversity: United States, Australia, Canada and Israel.

Difficult be build a "grand" model (800 variables) but possible to build lots of "huge" models

## Ensemble Effects

Best Model 8.4\%

Ensemble: 10.1\%

Rules: Once someone breaks 10\%, then the contest ends in 30 days.

## Enter "The Ensemble"’

23 teams from 30 countries who blended their predictive models who tried in the last moments to defeat BellKor's Pragamatic Chaos

## The Ensemble

"The contest was almost a race to agglomerate as many teams as possible," said David Weiss, a Ph.D. candidate in computer science at the University of Pennsylvania and a member of the Ensemble.
"The surprise was that the collaborative approach works so well, that trying all the algorithms, coding them up and putting them together far exceeded our expectations."

New York Times 6/27/09

## And The Winner is...

RMSE for The Ensemble:
RMSE for Bellkor's Pragmatic Chaos:
0.856714
0.856704

By the rules of the competition the scores are rounded to four decimal places so it was a tie.

However, BellKor's Pragmatic Chaos submitted 20 minutes earlier so they won. (and they had the lower error)

## Oh, by the way..

BellKor's Pragmatic Chaos
10.06\%

The Ensemble 10.06\%

50/50 Blend

## Problem Solving

## Diverse Perspectives

## Page vs de Marchi 3/17/98



Page
de Marchi

## Page vs de Marchi 3/17/98



Page

de Marchi
4.4
$\dagger \dagger$

## Page vs de Marchi 3/17/98



Page

$$
\begin{aligned}
& 4 \times 9 \\
& +i j
\end{aligned}
$$

## Page vs de Marchi 3/17/98

| * | $\stackrel{+}{*}$ | $\stackrel{+}{*}$ |
| :---: | :---: | :---: |


|  |
| :---: |

Page
de Marchi


## Page vs de Marchi 3/17/98




Page
de Marchi

$$
\begin{array}{cccc}
4 & \uparrow & \uparrow & \vdots \\
\hline
\end{array}
$$

## Page vs de Marchi 3/17/98




> Page
> de Marchi

## Page vs de Marchi 3/17/98



> Page
> de Marchi

## Page vs de Marchi 3/17/98



$9+4$
$i+4$
$\vdots$

> Page
> de Marchi

## A Magic Square

## Play it Again

Diverse Cognitive Models/Heuristics

## A Test

-Create a bunch of agents with diverse perspectives and heuristics
-Rank them by their performance on a problem.
-Note: all of the agents must be "smart"

## Experiment

## Group 1: Best 20 agents

Group 2: Random 20 agents
Have each group work collectively - when one agent gets stuck at a point, another agent tries to find a further improvement. Group stops when no one can find a better solution.

## The IQ View

Alpha Group


Diverse Group


# The diverse group almost always outperforms the group of the best by a substantial margin. 

See Lu Hong and Scott Page
Proceedings of the National Academy of Sciences (2002)

## The Toolbox View

Alpha Group


Diverse Group



## What Must be True?

Calculus Condition: Problem solvers must all be smart--we must be able to list their local optima

Diversity Condition: Problem solvers must have diverse heuristics and perspectives

Hard Problem Condition: Problem itself must be difficult

## Realizing Diversity's Benefits



## Out of the Bathtub and In the Group



Kevin Dunbar

## GRE:???




## Group Accuracy \& Perceived Effectiveness

Phillips, Lijjenquist, \& Neale, 2009


## Group Objective Accuracy vs Confidence in Decision

80
75
70
65
60
55
50
45
40


## The Prepared Mind



## The Prepared Mind Community



